

1 **Automatic measurement of shear wave splitting and**
2 **applications to time varying anisotropy at Mt. Ruapehu volcano,**
3 **New Zealand**

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Abstract

21 We present an automatic shear wave splitting measurement tool for local earthquakes,
22 with the sole manual step of choosing an *S* arrival time. We apply the technique to three data
23 sets recorded on Mt. Ruapehu Volcano in New Zealand that have previously been determined
24 to have fast polarizations that vary in time and with earthquake depth. The technique uses an
25 eigenvalue minimisation technique, applied over multiple measurement windows. The
26 dominant period of each waveform sets minimum and maximum window lengths. Cluster
27 analysis determines the best solution among all the windows, and quality grading criteria
28 assess the results automatically. When the same filters are used for events determined to be
29 high quality from manual studies, the automatic technique returns virtually identical results.
30 Scatter increases when the automatic technique chooses the best filter, but the average
31 automatic results remain consistent with the manual results. When the automatic technique is
32 used on sets that include data previously judged as poor quality, some stations yield
33 distributions of fast polarizations that include peaks that were not present in previously
34 published results. The difference may stem from two factors: automatic grading lets through
35 some measurements that independent analysts consider poor quality, but also unconscious
36 bias in the manual selection process may downgrade measurements that do not fit
37 expectations. Nonetheless, the new objective analysis confirms changes in the average fast
38 polarizations between 1994 and 2002, and between shallow and deep events. Therefore, this
39 new technique is valuable for objective assessment of anisotropy and its variation in time.
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41

42 **1. Introduction**

43

44 Seismic anisotropy, the directional dependence of seismic wave speed, is one of the few
45 means by which directionality can be measured beneath the surface of the earth. It has been
46 used widely to study strain and deformation due to aligned minerals in the mantle [*Fouch and*
47 *Rondenay, 2006; Savage, 1999*] and also to study structural properties and stress due to
48 aligned cracks in the crust [e.g., *Balfour et al., 2005; Boness and Zoback, 2006; Crampin,*
49 *1994; Zinke and Zoback, 2000*]. It has been proposed as a stress monitoring device that could
50 potentially have predictive powers for earthquake occurrence or volcanic eruptions [e.g.,
51 *Crampin, 1994; Gerst and Savage, 2004; Miller and Savage, 2001*]. To reach its full potential
52 for rapid evaluation in the case of monitoring, automatic methods are becoming imperative.
53 Manual measurements are time consuming and tedious, and they are less objective than fully
54 automatic methods.

55 The most common method to study anisotropy is to examine its birefringent effect on
56 shear waves, which is often called “shear wave splitting”. This splits the wave into
57 perpendicular fast and slow components. The first arriving wave has a polarization (ϕ)
58 parallel to the fast orientation of the anisotropic material and the delay time (dt) between the
59 two waves depends upon the integrated effect of anisotropy along the travel path. If
60 anisotropy is caused by alignment of near-vertical cracks or microcracks, then ϕ is a measure
61 of the average crack orientation, assumed to be parallel to the maximum horizontal stress
62 (S_{Hmax}) and dt is proportional to the crack density [*Hudson, 1981*].

63 Several techniques have been suggested for automatic analysis of shear wave splitting.
64 Many of them use as their basis the grid search technique pioneered by Silver and Chan
65 [1991] (SC91), which requires the user to select a time window over which to examine a
66 waveform. Their “eigenvalue” method is most relevant here; it is used when the incoming
67 polarization of the waveform is unknown. In this case, the pair of (ϕ, dt) that best returns the
68 waveform to linear particle motion as measured by the smallest eigenvalue of the corrected
69 covariance matrix is determined to be the best measurement.

70 The major difficulty of the SC91 algorithm is that the measurements can depend upon
71 both the filter used for analysis and also on the measurement window chosen. Several
72 approaches have been suggested for dealing with this. Walker et al. [2004] used the SC91
73 algorithm on SKS phases for 30 different time windows and averaged the results. A fully
74 automated method for SKS data uses at its base the SC91 algorithm [Evans et al., 2006]. It
75 uses a short term /long term average algorithm to pick the start of the SKS phase, and then it
76 measures splitting parameters on numerous windows to determine the set of windows with
77 the longest stable window length. However, 98% of the data are rejected with this method.

78 Other researchers use methods that are similar to the SC91 method, or incorporate parts of
79 it. For crustal events, Gao et al. [2006] and Bianco and Zaccarelli [2009] published semi-
80 automatic shear wave splitting methods that use the covariance matrix to determine the fast
81 polarization and cross correlation to determine the delay times. But they both require
82 extensive tuning of the parameters before applying the method to any particular dataset, and
83 use a fixed window length once the tuning is complete. Bianco and Zaccarelli [2009] used
84 their technique extensively on Italian volcanoes and document changes with time in the
85 polarizations and time delays. Peng and Ben-Zion [2004] also start with a method that is
86 equivalent to SC91. They choose a single frequency band (less than 15 Hz), and use a sliding
87 0.6 s long time window over the S arrival to determine which window yields the most linear

88 particle motion, which is used as their final determination. They also have a series of quality
89 criteria that they apply to weed out bad measurements. They tested their method with local
90 earthquake data recorded near the North Anatolian Fault, Turkey and report a rejection of
91 70% of the data. Liu and others [2007] use the SC91 method and also a cross correlation
92 method to determine splitting parameters for a large dataset. They also use a single filter (1-
93 10 Hz) and use a fixed start of 0.02 s before the *S* arrival. They use a variable window length
94 and choose the window that gives the maximum cross correlation coefficient as their best
95 window. Again, they have a number of criteria for grading the final measurements.

96 Teanby et al. [2004a] use a slightly different approach to find the best measurement
97 window. They use the SC91 method on multiple analysis windows and use cluster analysis
98 to determine the best measurement. The best measurement is determined to be within the
99 cluster that has the most measurements with the smallest error bars for the individual
100 measurements. This method has been systematically tested on a dataset in the North Sea and
101 proved useful for analysis of time variation of splitting using local events [*Teanby et al.*,
102 2004b]; and also for static properties of teleseismic events [*Greve et al.*, 2008; *Savage. et al.*,
103 2010], but most studies using this method include manual grading to weed out poor
104 measurements.

105 We present here a method for full automatic measurement of shear wave splitting that
106 allows the quick processing of thousands of events with minimal manual interaction. Our
107 method expands on the Teanby method by first finding the best filter and then using the
108 frequency of the seismogram to determine the lengths of the analysis windows. Using
109 multiple filters allows a larger set of data to be investigated than the previous techniques,
110 which mainly used single filters. We also developed an automatic grading technique that
111 evaluates the measurement based on the clustering characteristics instead of simply choosing
112 the best cluster. We have previously applied the method on earthquakes recorded at

113 volcanoes in Japan [*Savage et al.*, 2008; *Savage. et al.*, 2010], Alaska [*Johnson et al.*, 2010]
114 and Montserrat [*Roman et al.*, 2010], and we found time variations that we interpret to be
115 caused by deformation caused by magmatic movement. Here we present a detailed analysis
116 of the method and we apply it to data analyzed previously around Mt. Ruapehu Volcano,
117 from 1994, 1998 and 2002, in which temporal changes in anisotropy have been reported in
118 association with volcanic activity [*Gerst and Savage*, 2004; *Miller and Savage*, 2001].

119 **2. Method**

120 The method is based on the SC91 algorithm and the cluster analysis method of Teanby et
121 al. [2004a]. An overview of the processing steps is illustrated in Figure 1. Detailed
122 explanations are provided in the manual discussed in the appendix, and here we present a
123 summary. The SC91 analysis is carried out on multiple measurement windows and cluster
124 analysis determines the best window. The cluster that has the minimum variance is chosen as
125 the best cluster, and a final SC91 measurement is made based on the window that gives the
126 minimum error bars on the splitting parameters within the cluster. The main advance
127 presented here is in automatically choosing the range of the measurement windows to use for
128 the cluster analysis based on the period of the event. As part of this advance, we use multiple
129 filters to find the frequency bands with the best signals as measured by the product of the
130 signal-to-noise ratio and the filter bandwidth. Furthermore, automatic grading is carried out
131 to determine the best measurements. These extensions to the SC91 and Teanby et al [2004a]
132 techniques greatly simplify the processing of large datasets, with the only manual step being
133 in picking the S arrival time. However, the measurements require several parameters, which
134 could be checked and modified in other studies. These parameters can be easily changed in
135 the code and their definitions and choice of value are fully discussed in Table 2 of the manual.

136 **2.1 Filtering**

137 Since local broadband seismic data are often contaminated by noise, raw data can rarely
138 be processed. The application of a bandpass filter is important for shear wave splitting
139 measurements, because a sufficiently high signal-to-noise ratio is necessary for a high quality
140 measurement (Figure 2). However, narrow band filters should be avoided because they can
141 lead to cycle skipping. Therefore we favor broader band filters when possible. Instead of
142 applying a broad filter to all data or manually selecting a filter for each measurement, a
143 bandpass filter is determined for each measurement on the basis of a signal-to-noise ratio
144 criterion and the width of the filter, as discussed later.

145 A predefined set of 14 bandpass filters (Table 1), with typical corner frequencies found in
146 previous studies [*Gerst*, 2003] is tested for each measurement and the best filter is selected.
147 Using different filters would make this method applicable to broad classes of data beyond the
148 application to local *S* waves described herein. For example, the Teanby codes can be used on
149 teleseismic data to study mantle anisotropy [*Greve et al.*, 2008; *Savage et al.*, 2007] and
150 straightforward modifications of the codes described herein could be used to create automatic
151 *SKS* measurements. If short period data are used, the long period filters should be modified
152 since they will effectively be cut off at higher frequencies than expected, so some of the
153 resulting filters will give nearly identical responses. For particular datasets different sets of
154 filters may be more appropriate, although those listed in Table 1 provide reasonable starting
155 values for most microseismic studies.

156 **2.2 Signal-to-noise ratio calculation**

157 A new signal-to-noise ratio (SNR) for the filtered data is calculated using the same three
158 second window length for both noise and signal. The noise window precedes the *S* arrival
159 (here defined as time 0 s) and includes an offset to account for possible inaccuracies in the *S*
160 arrivals (here we use -3.05 to -0.05 s). The signal window follows the *S* arrival (here 0.05 to

161 3.05 s). The noise window is chosen to precede the S arrival directly to include the signal-
162 generated noise of the P coda, because such signal-generated noise will affect the S wave
163 analysis.

164 The mean of the ratio of the amplitude of the Fast Fourier Transform of the signal and
165 noise windows is used as the SNR. No measurements with SNR less than a maximum value
166 (3 here) are considered for interpretation. In the applications discussed herein, the
167 waveforms filtered with the three filters giving the highest value of the product of the filter
168 bandwidth in octaves and the SNR (if there are three or more filters fitting the SNR criterion)
169 are analyzed. This allows us to examine the frequency dependence of the results, and in
170 averaging the parameters, it ensures that the measurements that are most stable with
171 frequency contribute most to the final measurement. Earlier versions of the code used only
172 the SNR itself rather than the SNR-bandwidth product, and were more prone to cycle
173 skipping, relying more heavily on later grading to weed out poor measurements [*Johnson et*
174 *al.*, 2010; *Savage. et al.*, 2010].

175 **2.3 Basic splitting measurement technique**

176 The shear wave splitting parameters are measured by applying an inverse splitting
177 operator, which is determined by a grid search over possible values [*Silver and Chan*, 1991].
178 The more a certain operator removes the splitting of the investigated seismogram, the smaller
179 the second eigenvalue λ_2 of the covariance matrix of particle motion $c(\phi, dt)$ becomes. This is
180 equivalent to maximizing the linearity of the particle motion [*Silver and Chan*, 1991]. The
181 inverse operator that removes the shear wave splitting best gives the resultant shear wave
182 splitting parameters. Contours of λ_2 for all the operators considered give a measure of the
183 confidence region by using an F-test (SC91) (part f in Figure 3,4). Here we search the
184 parameter space in units of 1° and a time unit depending on the scale of the problem for all

185 fast polarizations and for delay times from 0.0 to a maximum value (*tlagmax*), 1.0 s in this
186 study. For some studies in which there were many local earthquakes close to a volcano, we
187 used a maximum of 0.4 s for the local events [*Johnson et al.*, 2010; *Savage et al.*, 2008;
188 *Savage. et al.*, 2010]. For *SKS* measurements, 4 to 6 s may be used [*Greve et al.*, 2008; *Savage*
189 *et al.*, 2007].

190 The results of the grid search for one pair of shear wave splitting parameters can be
191 dependent on the selected measurement window, i.e., the part of the waveform that is actually
192 considered for the measurement. To address this dependency, the analyst usually performs a
193 measurement several times with different measurement windows to confirm the stability of
194 the resulting parameters.

195 The method published by *Teanby et al.* [2004a] automatically performs measurements for
196 a large number of window configurations and then determines the most stable solution with
197 cluster analysis. The original method allows one to choose one set of configuration
198 parameters for all measurements or to interactively choose measurement window times. We
199 extended the method to automatically generate a customized configuration file for each single
200 measurement. Measurement window times relative to the *S* arrival are calculated based on the
201 dominant frequency of the signal.

202 The dominant frequency f_d is calculated from a window (3 s here) which follows the *S*
203 arrival. The maximum and minimum possible frequencies of f_d are limited such that at least
204 one full cycle is included in the calculation window and frequencies do not become
205 unfeasibly large. We used $0.3 \leq f_d \leq 8$ Hz.

206 Following suggested guidelines [*Teanby et al.*, 2004a], the minimum window (2-3 in
207 Figure 3b) to use in the splitting cluster analysis is chosen to be one period long (calculated
208 from $1/f_d$), while the maximum window (1-4) is 2.5 periods long. The number of different

209 measurement window end times depends on the minimum and maximum window length (see
210 the manual described in the Appendix for details). Here the number of end windows is
211 between 15 and 25.

212 The minimum and maximum times of the measurement window start are less critical than
213 the window end times [Teanby *et al.*, 2004a]. We consider five window start times in our
214 application of the cluster analysis, which are usually 0.2 s apart, so that $t=-0.3, -0.5, -0.7, -0.9$
215 and -1.1 s, relative to the S arrival. However, to minimize interference of the P wave for
216 close earthquakes, if the time between the S and P arrivals (T_s-T_p) is less than 2.2 s, we make
217 the shortest time window begin at $t=-0.1$ s and the longest time window begins at $-(T_s-T_p)/2$;
218 the other three time window start times are scaled accordingly. The total number of
219 measurement window N_{tot} is thus between 75 and 125, and is directly proportional to the
220 processing time.

221 The cluster analysis searches the parameter space of the N_{tot} pairs of measurements ($\phi(i)$,
222 $dt(i)$), where i is an index to indicate the measurement number, to determine clusters of
223 measurements with similar values, and is described more fully elsewhere [Teanby *et al.*,
224 2004a]. Several sets of statistics are used to describe the clusters, the most important of
225 which is the total variance of each cluster. It depends on both the average variance of the
226 individual measurements within each cluster and the variance of measurements within the
227 cluster. The cluster with the minimum total variance is chosen as the best cluster, and within
228 that cluster, the measurement with the minimum variance is chosen as the best measurement,
229 and is used as the final measurement for that phase at that filter. Measurements from
230 different filters are compared as discussed below.

231 **2.4 Grading criteria**

232 One problem plaguing shear wave splitting measurements is that of cycle skipping, in
233 which the splitting program may mismatch waveforms by an integer number of half-cycles. If
234 the waveform is mismatched by one half cycle, then the fast and slow waves may be
235 interchanged, and dt differs by one half period [e.g., *Matcham et al.*, 2000]. This is
236 particularly a problem with narrow band filters, and is a cause of concern at volcanic areas,
237 because the stress field near a dyke is proposed to reorient by nearly 90° after the intrusion
238 [*Gerst and Savage*, 2004]. Even when cycle skipping is not present, sometimes a cluster of
239 windows will include scattered phases that result in multiple solutions that differ from each
240 other by values that are other than an integer half cycle or 90° . For example, see Figure 4(c)
241 and (d), which has three groups of clusters with different ϕ and dt . Most studies use manual
242 checks to alleviate the problem, but it can be time consuming and also difficult to be
243 objective during manual checks. So we introduce an automatic technique instead to eliminate
244 measurements with multiple solutions.

245 We automatically grade the measurements based on the cluster analysis. Instead of simply
246 using the results from the best cluster, all clusters with measurement numbers above the
247 minimum threshold are compared to the chosen “best cluster”. We try to reject
248 measurements in which there are secondary clusters with similar quality to the best cluster,
249 but with very different shear wave splitting parameters. Let $var(k)$, $\phi(k)$, $dt(k)$, and $Nmeas(k)$
250 be the average variance, fast polarization, delay time, and number of measurements in cluster
251 k , respectively. Let $kbest$ be the cluster number of the measurement with $var(kbest) =$
252 $min(var(k))$. This is the cluster chosen by the original Teanby et al. [2004a] program to be
253 the best measurement. $Nmeas(kbest)$ is thus the number of measurements in the best cluster.
254 To consider clusters of similar quality, the cluster grading considers all clusters with $var(k)$
255 $< 5 * var(kbest)$. Within these “OK clusters” we consider the differences between the fast
256 polarizations and delay times of each cluster compared to the best cluster. Therefore, we

257 define $\phi_{diff} = \text{abs}(\phi(k) - \phi(k_{best}))$ and $dt_{diff} = (dt(k) - dt(k_{best}))$ to assess the reliability of the
258 best cluster. Table 2 includes a description of the cluster grading methods.

259 Another concern is for “null” measurements, which can occur when there is no anisotropy
260 in the plane of the S wave particle motion, or when the initial shear wave is polarized along
261 the fast or slow orientation of the medium, so that no orthogonal wave exists to split (Figure
262 5; see also [*Silver and Chan, 1991; Wüstefeld and Bokermann, 2007*]). Often they will be
263 given a poor grade in the cluster grading since different windows may return ϕ or dt that are
264 far apart. But in case the cluster grading has not removed them, these null measurements are
265 treated separately from regular splitting measurements. We use a geometrical criterion [*Peng*
266 *and Ben-Zion, 2005; Savage et al., 1996*]; we compare the initial polarization α determined
267 from the SC91 inversion program to the fast polarization ϕ . Measurements are considered as
268 null, if they do not fulfill the criterion $20^\circ \leq |\phi - \alpha| \leq 70^\circ$. For a uniform distribution of
269 incoming polarizations, we expect 4/9 of the measurements to be rejected by this criterion.

270 Measurements that result in a delay time close to the maximum indicate cycle skipping or
271 noisy data [*Evans et al., 2006*], therefore measurements close to the maximum dt are also
272 rejected. The mean delay time obtained by Gerst and Savage [2004] for local earthquakes at
273 Mt. Ruapehu in 2002 is 0.11 s for shallow events ($z < 35$ km) and 0.27 s for deep events ($z > 55$
274 km). For local events the delay times are generally expected to be between 0.1 and 0.6 s
275 (Table 1 of Savage [1999]). Therefore we choose the maximum delay time for the grid
276 search (t_{lagmax} described above) to be 1.0 s and subsequently rejected all measurements
277 with a delay time greater than 0.8 times this value. A final grade of A or B is made based on
278 whether the measurement has a cluster grade of Acl or Bcl , and values of the SNR and 95%
279 confidence interval of the ϕ measurement (Table 2).

280 Finally, we developed a criterion based on our manual grading techniques, which involve
281 examining the plots of the contours of the eigenvalues of the covariance matrix of the final
282 best measurement (e.g., Figures 3, 4 (f)). A small range of contours indicates that the best
283 result is not much better than the worst result. Within the SC91 code, the eigenvalues are
284 rescaled so that the 95% confidence interval has a value of 1 and contours are multiples of
285 this interval. We use the maximum value of the error contours as a further grading parameter.
286 This quantity is correlated with the signal-to-noise ratio, and on the formal error bars of the
287 final best splitting measurement, which we also include as grading criteria (errors in ϕ must
288 be less than 25° for quality A and B measurements), and which is also based on the contours.
289 But the energy criterion is distinct, as it applies to the whole error surface, not just the region
290 around the minimum. Below we use a value of 8 or greater of the maximum error contour to
291 define a high quality measurement (Eng8). The value of 8 was chosen because it left roughly
292 the same number of measurements in the high quality manual (A and B) and the automatic
293 technique in an early implementation of the SNR criteria.

294 The manual results against which we compare our data were hand graded with published
295 results ranging from C to A, including half-grades [*Gerst*, 2003]. It is difficult to exactly
296 match hand graded versus automatic grades. However, the measurements graded A and AB
297 in Gerst [2003] have similar results to those graded A and B in our analysis (see below); we
298 show below that when they are used on the same waveforms, they give closely matched
299 results. Therefore we consider that the automatic A and B analysis is similar to the A and AB
300 manual grades.

301 **2.5 Averages**

302 To calculate average parameters over multiple events sampling the same anisotropy, we
303 use Gaussian statistics for the delay times, and the Von Mises criterion [*Mardia*, 1972], a

304 circular analogue to the normal distribution, for the polarizations. Along with the calculation
305 of a mean fast polarization, a test for non-randomness must be conducted [Davis, 1986]. The
306 calculation for the mean of the polarizations involves adding unit vectors with orientations
307 given by the measured values and dividing by the number of measurements. The ambiguity
308 of 180° in polarization is taken care of by doubling the angles before the vector addition, and
309 halving the resultant angle. The length of the resultant vector, R , gives a measure of the misfit
310 between 0 and 1. $R=1$ when all the polarizations are exactly lined up. Errors presented are
311 the standard error, which is valid if the distributions are approximately normal. However,
312 many of the distributions are bimodal and thus are not well described by normal distributions,
313 so we recommend caution in using the averages and standard errors.

314 **2.6 Use of multiple filters**

315 Several of our earlier studies presented results from the same event-station pair using
316 multiple filters in the rose diagrams and used these multiple filters in the averages. The
317 rationale was that if an event had the same results with different filters, including it several
318 times would effectively weight the results more heavily than if it had different results with
319 different filters. However, such results should not have been treated with Gaussian statistics
320 because the results from different filters will correlate with each other. It is also difficult to
321 decide which filter results to compare with each other. Therefore, unless otherwise noted, for
322 the measurements shown here we include a further step, which is effectively another grading
323 step: for a given event-station pair, if more than one filter produced a result that has passed
324 the grading criteria, we compare the results and remove the entire measurement if they are
325 too different from each other, using the criteria described above for the cluster grading, i.e., if
326 the time difference is greater than one eighth the maximum allowed value or if the angular
327 distance is greater than $\pi/8$. If the results are similar, we choose the one with the smallest
328 error bars, as calculated by the sum of the relative errors.

329 3. *Data*

330 The method presented here can generally be used to perform shear wave splitting
331 measurements on any three-component data with *S* phases that are discernable above the
332 noise. Because different measurement windows are processed by the cluster analysis, and
333 because the windows begin a set time before the *S* phase, small errors in the *S* arrivals are
334 mitigated.

335 The cluster analysis method was extensively tested and compared with manual
336 measurements [*Teanby et al.*, 2004a]. In the initial development stage of the modified method
337 [A *Wessel*, 2008], we used the manual results from sixteen high quality events recorded at
338 four stations of the 2002 CHARM deployment on Ruapehu [*Gerst*, 2003; *Gerst and Savage*,
339 2004] to guide our choice of the best parameters to try to match the manual results. The
340 method was further developed to work at Asama volcano in Japan. Filters were changed
341 slightly from the original study. Because many of the seismograms were emergent at Asama,
342 we used a longer window before the *S* arrivals, which we carry over into the analysis here.
343 We also developed the grading technique by examining data recorded at Asama to find the
344 most stable results [*Savage. et al.*, 2010].

345 To test the newly developed method, we used data that were recorded by temporary
346 deployments in 1994, 1998 and 2002 on Mt. Ruapehu Volcano, New Zealand, and which
347 were already analyzed manually [*Gerst*, 2003]. The data sets from 1994 and 1998 were
348 sparse (5 and 3 stations, respectively), while 8 stations contributed data in 2002. All *S* phases
349 used in the automatic processing for comparison to the manual methods were re-picked
350 manually, because the previously processed data [*Gerst*, 2003; *Gerst and Savage*, 2004] did
351 not indicate the *S* arrivals, but only the window about the *S* wave used in the final analysis.
352 Events are separated into shallow ($z \leq 35$ km) and deep ($z \geq 55$ km) events. Only the 1994 deep

353 and 1998 shallow events were reprocessed manually to compare to the 2002 dataset [*Gerst*
354 *and Savage, 2004*], and so we do not include the 1994 shallow or 1998 deep events processed
355 in an earlier study [*Miller and Savage, 2001*].

356

357 **4. Results**

358 **4.1 Comparison of individual measurements**

359 Figure 6 presents the distribution of the frequencies used in the analysis, by plotting
360 histograms of the numbers of measurements as a function of the dominant frequency in the
361 measurement window. Before filtering, the distribution of the dominant frequencies is
362 relatively uniform between 2 and 7 Hz. The measurements with the best signal-to-noise ratio
363 tend to come from filters with lower frequencies, so that the dominant period of the
364 seismograms for most measurements is 3 Hz. The dominant frequencies of the data filtered
365 with the best SNR-bandwidth product also have a peak at 3 Hz, but there are more
366 measurements at higher frequencies than when the SNR alone is used.

367 We performed several tests of the method. First, we selected the measurements for the
368 2002 data determined by Gerst [2003], that had A and AB ratings, and compared these
369 manual results to the automatic results using the same filters on the same waveforms (Figure
370 7; Table 3). The difference between the two methods is that the automatic program chooses
371 the best window by cluster analysis, while the manual method relies on a human to test
372 several windows and filters. If two or three filters gave different results they are all included
373 in the analysis.

374 The results are shown for increasing levels of grading (Table 2; section Methods). The
375 scatter in the relation increases when poorer quality data are used, but the number of data
376 points is increased (Figures 7, 8, Table 3). However, the majority of all the measurements are
377 within 25 degrees (minimum 75%) and 0.2 s (minimum 85%) of each other, even when no
378 quality criteria are applied (Table 3). The "Energy contour ratio > 8" (Eng8) criterion seems
379 to get rid of almost all outliers once all the other criteria have also been applied (Figure 7).
380 But it does this by leaving out many more measurements. The "all" or "unculled" group (no
381 quality criteria applied beyond the original Teanby et al. methodology) has 212
382 measurements, reducing to 160 when the null criteria and the D quality measurements from
383 clustering are left out (noNnoD). The AB group, which are the quality that were used in
384 previous publications [*Johnson et al.*, 2010; *Savage. et al.*, 2010], have 145 measurements
385 and when only the top "A" quality measurements and the "Eng8" criteria are applied it
386 reduces to 75, leaving out almost 2/3 of the measurements. Interpreting this must be
387 tempered by the fact that we chose the "Eng8" criterion in order to get roughly the same
388 number of measurements as were in the A and AB manual measurements in an earlier version
389 of the codes.

390 Another test is to see whether the results will be the same if the automatic code chooses
391 the filter. We compare the same A and AB measurements from Gerst [2003], but allow the
392 automatic program to choose the filters based on the signal-to-noise ratio-bandwidth criterion
393 (Figure 9, Table 3). Both the automatic and manual analyses sometimes give different results
394 for different filters. We have applied the criterion described above separately to the manual
395 measurements and the automatic measurements to weed out measurements that have different
396 results at different filters, so that we compare only one measurement for each event-station
397 pair. Surprisingly, there are fewer outliers for this case compared to when we used the exact

398 same filters, and there is less difference between the various grading criteria; we discuss the
399 reasons below in the discussion section.

400 Using three filters requires more computer processing time, and in monitoring situations it
401 would be preferable to have a rapid evaluation. Therefore we test the results for the best
402 single filter compared to the manual results (Figure 10). As in the case when the exact filters
403 were compared (Figure 7), increasingly higher quality criteria lead to smaller scatter at the
404 expense of leaving out more measurements. In this case the “ABeng8” criterion reduces the
405 results to 33 from 116 measurements, or 28% of the total.

406 Finally, we apply the most rigorous test, which is to start with all quality data rather than
407 the selected A and AB quality measurements to see if our technique leaves out the same
408 events and gives the same results (Figure 11; 12, Table 4). This test most closely matches the
409 envisioned applications, when investigators will be using the automatic techniques to
410 evaluate data that has not yet been examined. We started with all the data that had splitting
411 measurements made by Gerst [2003], including the null measurements (431 measurements).
412 We ran the automatic method on these phases, allowing the automatic technique to choose
413 the best filter and keeping the results from the best three filters if they passed the other
414 quality criteria. Rose diagrams made with measurements fitting the ABeng8 criterion (162
415 events) are compared to the A and AB quality non-null measurements determined by Gerst
416 (168 measurements) (Figure 11, 12). Table 4 compares the results separated into years and
417 deep and shallow events for several methods of measurements compared to the manual
418 results. The rose diagrams use results from all three filters in all studies because they most
419 closely match the conditions used by Gerst and Savage [2004]. The tables present more
420 results using our selection technique to only choose one filter in each measurement set, for
421 both the original AB files and those with eng8.

422 **4.2 Comparison of averages**

423 In all cases, the automatic results are less coherent than the manual ones, as measured by
424 smaller values of R (Table 4). The mean for all delay time measurements in each depth group
425 differs by less than 0.04 s for manual vs. automatic, although in a few cases they are slightly
426 beyond the 95% confidence interval for the hypothesis that they are taken from the same
427 population. The delay times in the deep groups are significantly larger (around 0.25 s) than
428 the shallow group (around 0.14 s). The most scattered results, with the smallest R , are for the
429 1998 shallow events in all groups. 1998 and 2002 automatic measurements are within the
430 95% confidence intervals of the manual ones, but the automatic measurements for 1994 deep
431 are more northerly (-25 ± 6) than the manual measurements (-43 ± 4). For the most
432 numerous 2002 dataset, the biggest differences between the manual and automatic results are
433 for deep events at stations LHUT2 and FWVZ (Figure 11).

434 **5. Discussion**

435 **5.1 Comparison of Individual Measurements-Scatter Plots**

436 As discussed in Section 4.1, when the automatic technique chooses the best filters, the
437 measurements are slightly more scattered, but the average values are close and surprisingly,
438 there are fewer outliers than when the exact same filters are used (compare Figs. 7 and 9;
439 Table 3). The results for different quality criteria are also somewhat unexpected, because
440 there are fewer measurements in the group without quality control applied (“all or unculted”),
441 than some of the others. To understand this, recall that the quality criteria are applied before
442 the program that determines whether measurements at different filters should be discarded.
443 So for the “unculted” measurements, if a poor quality result at one frequency gives a different
444 answer than a higher quality result, all the results for that event/station pair are thrown out.

445 On the other hand, in the "culled" plots, we first get rid of measurements with poor quality
446 criteria, e.g., if an individual measurement at one frequency has too high error bars, it will be
447 thrown out and the other two measurements will be left to compare to each other to see which
448 one is kept for the final figure. This suggests that an effective way of removing poor
449 measurements may be just to measure results on the three best filters and compare the results,
450 without doing any of other quality checking.

451 Delay times from shear wave splitting measurements from local events generally yield a
452 high scatter of approx. 80%, and the large range of delay times in our data confirms this
453 [*Crampin, 1999; Gerst and Savage, 2004*]. Nonetheless, delay times are consistent between
454 the manual and automatic method (Fig. 7-10). Therefore, the scatter in delay times is not a
455 function of processing errors, but must result from some physical process. That process
456 could be rapid stress changes occurring between each measurement [*Crampin et al., 2004*],
457 but we think that is unlikely, especially since there is a scatter for measurements made at a
458 single waveform but at different frequencies. Instead, phases converted or scattered from
459 interfaces with strong velocity contrasts, such as magma pockets, could be arriving before or
460 after the initial wave and interfering with some of the measurements. In this case, slight
461 changes in paths could make a change in the splitting measurement [e.g., *Liu et al., 2004*].

462 The histograms of differences between manual and automatic results (Figs. 8,9) do not
463 show a strong signal from peaks at 90 degrees, suggesting that cycle skipping is not a
464 problem with this data.

465 **5.2 Comparison of Individual Stations-Rose Diagrams**

466 Despite the close relationship when comparing waveforms already judged as high quality
467 by the manual method, if all data are included in the processing, histograms of fast
468 polarizations of the top quality automatic measurements vary at some stations compared to

469 the manual measurements (Figure 11; Figure 12). Results and result qualities vary from
470 station to station in both data sets. In particular, at most stations the automatic measurements
471 are more scattered than the manual measurements, although some stations (e.g., LHOR;
472 FWVZ shallow) have less scatter with the automatic than with the manual methods (Figure
473 11).

474 Hypotheses for differences that we have explored are (a) the different techniques reject
475 null measurements at a different rates (b) manual analysis is better than automatic at leaving
476 out nulls and mismatched phases (c) the manual analysis is unintentionally biased. The
477 proportions of nulls rejected are similar for the automatic (15%) versus manual (20%), so (a)
478 is not the answer. Hypotheses (b) and (c) are examined by detailed analysis of waveforms
479 and their grading at two key stations, using plots such as those in Figure 3 and 4 (Table 5).
480 The biggest differences between manual and automatic measurements occurred for station
481 LHUT2 for the 2002 deep measurements (Figure 11). LHUT2 has a single NE/SW peak in
482 the manual measurements, but an additional second peak in the rose diagrams for the
483 automatic methods makes them bipolar. The new automatic technique gives three
484 measurements for two events with values between -81 and -85 ("E-W" measurements), with
485 the rest of the results spread between 22 and 65 (Table 5). The manual measurements gave
486 similar values for the two "E-W" measurements reported, of -71 and -88. But only one filter
487 instead of two was judged high quality for one of the measurements, and the other was
488 graded B, so it was left out of the A/AB plot. More measurements were graded high that
489 gave results between 10 and 70 degrees. Some but not all of these measurements had dt
490 values that were less than 0.1 s (Tables 3, 4), which could be indicative of small anisotropy
491 that could easily have polarizations change. The filters chosen by the automatic method had
492 overlapping frequency bands, which could bias them by allowing multiple measurements
493 with the same values. However the filters used in the manual technique also had overlapping

494 frequency. Finally, earlier versions of the automatic routine that used the SNR alone instead
495 of the SNR-bandwidth product had stronger bimodality in the solutions than the SNR-
496 bandwidth product (Figure 11, 12), which suggests that the bimodality could be caused by
497 cycle skipping. So we conclude that both factors (b) and (c) may be playing a role in the
498 differences: there may be some unintentional bias in the manual determination that rejected
499 more measurements that did not fit the expected polarization, but the manual grading may
500 also be better able to reject poor or marginal measurements. We think that it is natural for
501 manual graders to tend to favor measurements that are consistent with previous
502 measurements at the same station, leading to a narrower scatter for manual measurements
503 than for automatic ones. Table 5 shows that two independent observers do not always grade
504 the same measurement the same way.

505 **5.2 Average results and time variations**

506 The average results across all stations for the 2002 data are similar for the manual and
507 automatic measurements (Figure 11; Table 4). Although the 2002 shallow events have
508 average results that differ between manual and automatic measurements by more than the
509 standard error, the absolute difference between the manual and automatic techniques is less
510 than 10° . The biggest difference in the average results over all stations for the manual vs.
511 automatic techniques occurs for the shallow measurements in 1998, which had almost twice
512 as many automatic as manual measurements, and the averages differ by 52° . The differences
513 are not too surprising, however, if we consider that the main conclusion about the 1998
514 shallow events was that they were more scattered than the 1998 deep events or than the 1994
515 measurements from earthquakes at all depths [Miller and Savage, 2001].

516 For the automatic technique, differences in the average fast polarizations between the
517 1994 deep events and the 1998 shallow events are not statistically significant, but the

518 difference between 1994 deep events and 2002 deep events (59 ± 19) is robust (Table 4).
519 Differences in average ϕ in 2002 between shallow and deep events that were pointed out
520 Gerst and Savage [2004] are not as strong with the automatic technique, but they are
521 statistically significant (differences are 37 ± 12). Therefore, spatial and time variations of
522 seismic anisotropy are confirmed for Mt. Ruapehu when a fully objective, automated method
523 is used.

524 The stations that had the most scatter in 2002 are close to each other (Figure 11), near the
525 summit of Mt. Ruapehu. We are presently operating another network to study spatial
526 variation of anisotropy on Mt. Ruapehu, which might help to clarify whether this is a trend.

527 **5.3 Recommendations:**

528 The method can in principal be used with any three-component local earthquake data set.
529 So far it has been tested on other data sets on Mt. Asama volcano [*Savage. et al., 2010*] and
530 three other volcanoes in Japan [*Savage et al., 2008*], Okmok, Alaska [*Johnson et al., 2010*]
531 and at Soufriere Hills volcano in Montserrat [*Roman et al., 2010*]. But we have also made
532 some preliminary studies in non-volcanic areas of New Zealand and have found it to work
533 equally well. With changes in filters we expect that it could readily be modified for
534 teleseismic events, because the original Teanby code has already been modified for
535 teleseismic analysis [*Savage et al., 2007*].

536 If there is plenty of time for analysis such as when real-time applications are not being
537 used, then since the shapes of the histograms for different quality criteria don't change too
538 much with respect to outliers (Figure 9; 10), it would be best to keep the results that give the
539 most total measurements, i.e., in this case the three filters with the "AB" criteria (86
540 measurements). However, using only the best "fb1" filter yields almost as many (80)

541 measurements, and will take only 1/3 as much processor time. Therefore it is certainly
542 acceptable in real-time analysis, and may also be reasonable for other applications. Using the
543 “energy >8” criterion reduces outliers almost to zero, but it also reduces the measurements
544 considerably and is probably only acceptable in situations where there are large quantities of
545 measurements to choose from, such as when time variations are not observed. Using a
546 smaller level for the energy contour grading criteria could also be explored.

547 We expect that in different areas, different filters might be more suitable. It should be
548 simple to customize the filters for different regions (see details in the manual discussed in the
549 Appendix).

550 Visual analysis of waveform fits will be necessary in any study in a new area to check
551 that the parameters used in the automatic techniques are suitable. We recommend that in new
552 studies, manual results for a subset of events first be checked against the automatic results
553 and that several sets of parameters be tried and adjusted before the automatic technique is
554 used on the rest of the data. The method may need to be customized for some studies to
555 allow more or less scatter, and special studies may wish to use hand grading. But this new
556 technique should be valuable for rapid and objective overall assessment of anisotropy and its
557 variation in time.

558

559 ***6. Conclusions***

560 The automatic technique returns results that are nearly identical to manual techniques
561 when used on equivalent datasets. Scatter increases when the automatic technique chooses
562 the best filter and increases more when it is used on data previously judged as poor quality.
563 This scatter is caused mainly by the manual and automatic grading assigning different

564 qualities to the same measurements. Some of the difference in quality may stem from a
565 better ability to reject unsuitable waveform fits by a visual analysis, but some may stem from
566 an unconscious bias in manual grading, which downgrades measurements that do not fit
567 expectations. The new objective analysis confirms changes in the average fast polarization
568 between deep events at Mt. Ruapehu in 1994 and 2002, and between shallow and deep events
569 in 2002.

570

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- 680

681 Figure Captions.

682 Figure 1. Flowchart of data processing steps. Dashed lines are optional steps.

683 Figure 2. Comparison of waveforms after the application of different bandpass filters.

684 Although a change in frequency content is visible on the top trace (raw data), the *S*-wave is
685 masked by long period noise. The application of a bandpass filter (BP) emphasizes the signal,
686 but the narrow 2-3 Hz filter appears “ringy” and is susceptible to cycle skipping. (a) small
687 event ($M=3.8$) recorded at station LHOR. The best filters as measured by the maximum of
688 the product of the SNR and the bandwidth (fb1 through fb3) are at high frequencies, but the
689 best frequency still has a narrow 1-Hz bandwidth. (b) larger event ($M=4.2$), which has better
690 response at long periods.

691 Figure 3. High quality, A grade (Table 2) measurement recorded at station LHOR for a
692 regional event. The grey boxes in panels (a), (b) and (e) delineate the time window used for
693 the final measurement. (a) filtered East (E) North (N) and vertical (Z) waveforms. The solid
694 line is the *S* arrival. The dashed lines are the minimum start (1) and maximum end (4) times
695 for windows used in the processing, as in (b). (b) the waveforms rotated into the SC91-
696 determined incoming polarization direction (p) and its perpendicular value (p^\perp), for the
697 original filtered waveform (top) and the waveforms corrected for the SC91-determined dt
698 (bottom) for the window shown in grey. The straight black line is the *S* arrival. The two sets
699 of dashed lines on either side of the straight line show the range of allowed starting (1 and 2)
700 and ending (3 and 4) windows for the SC91 measurements. (c) ϕ and dt determined for each
701 measurement window as a function of window number. (d) all the clusters of 5 or more
702 measurements, with the large cross being the chosen cluster. (e) waveforms (top) and particle
703 motion (bottom) for the original (left) and corrected (right) waveform according to the final

704 chosen SC91 window. (f) contours of the smallest eigenvalue of the covariance matrix for the
705 final chosen SC91 measurement.

706 Figure 4. Sample C quality measurement, as in Figure 3. This sample presents good
707 waveform fits and has a high signal-to-noise ratio for the best measurements, but other
708 windows with qualities that are not much different have ϕ that vary by tens of degrees, so the
709 measurement may exhibit cycle skipping. We do not analyse this grade of measurement.

710 Figure 5. Null measurement: an unsplit shear wave shows a lack of energy on the
711 component perpendicular to the initial polarization.

712 Figure 6. Histograms of dominant frequencies in the measurement windows used in the
713 analyses. (a) defining the best filters by using only the maximum SNR, (b) defining the best
714 filters by comparing the product of the SNR and the filter bandwidth. (c) The raw, unfiltered
715 data.

716 Figure 7. Comparison of manual vs. automatic measurements of fast polarizations (a) and
717 delay times (b) for all stations, using the same filters in both studies (the filters used are those
718 determined by Gerst & Savage (2004) qualitatively to yield the best measurements), and
719 showing results using different quality criteria in each box (Table 2; 3). Note that wrap-
720 around effects make the measurement at (80, -85) appear to be far apart, while in fact they
721 differ by less than 15° . The headings are defined in Table 2.

722 Figure 8. Histograms showing the distribution of differences between ϕ for the manual
723 and automatic measurements in Figure 7. The histograms all have the same scale.

724 Figure 9. Comparison of 2002 measurements from automatic and manual methods,
725 allowing the program to choose the filters based on the SNR and the set of 14 filters that are

726 shown in Table 1. Only the “AB” and “AB eng8” sets (Table 2; 3) results are plotted. Again,
727 most of the measurements lie close to the 1-1 line. (top) comparison of ϕ values. (middle)
728 comparison of dt values. (bottom) histograms of the difference between the automatic and
729 manual measurements of dt , all using the same scale.

730 Figure 10. Scatter plots of measurements from the single best filter compared to the
731 manual measurements, for no culling, using the “AB” criterion, and the “AB eng8” criterion.
732 (top) comparison of ϕ values. The number of measurements in each plot is given in the upper
733 left hand corner. (bottom) comparison of dt values.

734 Figure 11. Rose diagrams of manual and automatic results compared at each station.
735 Plots on left are manual, middle are automatic based on using filters fitting the SNR criteria
736 alone and plots on right are automatic using the SNR-bandwidth product to determine which
737 filters are best. Top is for events with depth < 35 km. Bottom is for events with depth > 55
738 km. Up to three different filters per event are included. This is to account for the relatively
739 sparse data set.

740 Figure 12. Same as Figure 11, but for 1994 deep and 1998 shallow results.

741

Table 1. Filters tested

Filter number	Low freq (Hz)	High freq (Hz)	Bandwidth (octave)
1	0.4	4	5
2	0.5	5	5
3	0.2	3	7.5
4	0.3	3	5
5	0.5	4	4
6	0.6	3	2.5
7	0.8	6	3.75
8	1	3	1.5
9	1	5	2.5
10	1	8	4
11	2	3	0.75
12	2	6	1.5
13	3	8	1.3
14	4	10	1.25

Table2. Quality Criteria

Grade name	Criterion
N (null)	If the fast polarisation f is between -20 to 20 or 70 to 110 degrees of the incoming polarization
Dcl	Cluster D grade: If there is any cluster k for which the following holds: $nmeas(k) > Nmeas(kbest)/2$ and $var(k) < 5 var(kbest)$ and also: $(tdiff(k) > tlagmax/4$ or $(\pi/4 < phidiff(k) < 3\pi/4)$)
Ccl	Cluster C grade: If the cluster is not D grade and there is any cluster i for which the following holds: $nmeas(k) > Nmeas(kbest)/2$ and $var(k) < 5 var(kbest)$ and also: $tdiff(k) > tlagmax/8$ or $\pi/8 < phidiff(k) < 7\pi/8$.
Bcl	Cluster B grade: If the cluster is not grade D or C and there is any cluster k for which the following holds: $var(k) < 5*var(kbest)$ and $nmeas(k) > Nmin$ (5 here) and also: $tdiff(k) > tlagmax/8$ or $\pi/8 < phidiff(k) < 7\pi/8$
Acl	Cluster A grade: If the cluster is not grade D or C or B
ABPAR	based on parameters alone: not null, $dt < 0.8*tlagmax$, $SNR > 3$, $d\phi < 25$
APAR	based on parameters alone: $dt < 0.8*tlagmax$, $SNR > 4$, $d\phi < 10$, where $d\phi$ = standard deviation of ϕ
B	Cluster B, not null, $dt < 0.8*tlagmax$, $SNR > 3$, $d\phi < 25$
A	Cluster A, $dt < 0.8*tlagmax$, $SNR > 4$, $d\phi < 10$
AB	A or B
Eng8	As described in text, maximum value of contour energy plots is greater than 8

Table 3. Comparison of Measurements for different quality criteria.

Method of culling	Total number of events	Proportion Of total (%)	Number within 25 deg	Proportion within 25 deg(%)	Number within 0.2 s	Proportion within 0.2 s (%)
Compare same filters						
All meas	212	100	158	75	181	85
NoN (No Null meas.)	179	84	157	88	166	93
NoD (No meas. with DCI)	178	84	151	85	163	92
NoN, NoD	160	75	142	89	151	94
NoN, dt<0.8	175	83	153	87	164	94
NoN, dt<0.8, SNR>3	169	80	146	86	157	93
NoN, dt<0.8, SNR>3, $d\phi < 25$	169	80	146	86	157	93
NoN, dt<0.8, SNR>4, $d\phi < 10$	137	65	123	90	134	98
AB	145	68	131	90	138	95
A	110	52	101	92	107	97
ABeng8	88	42	87	99	87	99
Aeng8	75	35	74	98	75	100
Compare different filters						
All filts (3 best)	77	100	67	87	72	94
AB (3 best)	86	112	73	85	80	93
AB eng 8	56	73	52	93	54	96
fb1	116	100	93	80	96	83
fb1 AB	80	69	74	93	76	95
fb1 AB eng8	33	28	32	97	33	100

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Table 4. Average results from the 1994 and 1998 and 2002 deployments (all stations)

Data set	Method	ϕ [°]	$\pm \phi$ [°]	δt [s]	$\pm \delta t$ [s]	R	#
1994 deep	Automatic-up to 3 filters ABeng8	-29	4	0.24	0.02	0.65	44
	Automatic best meas of 3 filters	-25	6	0.26	0.03	0.46	43
	Auto eng8 then best of 3	-25	7	0.26	0.04	0.54	26
	Manual	-42.8	3.6	0.23	0.021	0.707	37
1998 shallow	Automatic up to 3 filters ABeng8	-13	11	0.13	0.009	0.2	79
	Automatic AB best meas of 3 filters	-18	14	0.16	0.01	0.14	101
	Auto eng8 then best of 3	-5.2	16	0.14	0.01	0.17	49
	Manual	13.4	5.8	0.11	0.0093	0.516	39
2002 deep	Automatic up to 3 filters ABeng8	10	6	0.24	0.02	0.4	62
	Auto AB best of 3 filters	26	10	0.29	0.02	0.23	72
	Auto eng8 then best of 3	10	7	0.24	0.025	0.43	37
	Manual	19.2	2.7	0.272	0.016	0.63	117
2002 shallow	Automatic up to 3 filters ABeng8	-17	5	0.12	0.008	0.41	100
	Auto AB best of 3 filters	-16	6	0.14	0.009	0.35	100
	Auto eng8 then best of 3	-16	7	0.13	0.01	0.37	58
	Manual	-30	2.4	0.107	0.0048	0.69	123

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Table 5. Comparison of manual and automatic measurements at station LHUT2 [i].

EQ ID	filter (Hz)	dt (s)	ϕ ($^{\circ}$)	Auto grade	pick grade	Gerst dt	Gerst ϕ	Gerst grade	new grade
2002.126.20	0.5-5	0.06	-85	BCI	1	0.05	-71	B	1
2002.126.20	0.1-2					0.1	24	A	
2002.125.17	0.1-3	0.1	22	ACI	2			X	1
2002.125.17	2.0.6-3	0.1	26	ACI	2	0.1	31	A	1
2002.132.04	0.2-2					0.1	23	nullA	
2002.132.04	0.4-4	0.31	38	ACI	1	0.5	39	AB	1
2002.132.04	1-3					0.5	33	C	
2002.015.09	0.4-4	0.3	59	ACI	1	0.28	54	AB	1
2002.015.09	0.5-5	0.28	60	ACI	1			X	1
2002.016.12	0.3-3	0.28	65	ACI	1	0.1	39	AB	1
2002.073.02	0.1-8	0.14	-85	ACI	1	0.05	-88	AB	1
2002.073.02	1-5	0.14	-81	ACI	1			x	1

[i]All measurements for deep events with automatic grades A or B and energy contour greater than 8 are included. Manual measurements are reported in the same line as the closest automatic measurement. If there were more manual measurements than automatic for an event or vice versa, an extra line is included with the single measurement. Measurements are sorted by fast polarization. Column Auto Grade gives the grades determined by the automatic grading described in Table 3. Column Pick grade is the grade given during manual picking of the S wave and represents how well the analyst thought the S wave arrival time was determined (1=good, 2=fair). Columns labeled "Gerst" were grades determined by Gerst [2003] (X=not used). Column labeled "new grade" is for grades determined by Teanby before he had read an initial version of the manuscript and was invited to be an author, so we consider him to have been an independent observer.

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751 **Appendix**752 **Obtaining and using the programs**

753 The codes for this method have mainly been written in BASH syntax, SAC scripts

754 [*Goldstein and Snoke, 2005*], Fortran and GMT [*P Wessel and Smith, 1991*] and all necessary

755 programs are freely available. The programs and a detailed technical manual can be found

756 online (<http://mfast-package.geo.vuw.ac.nz/>).

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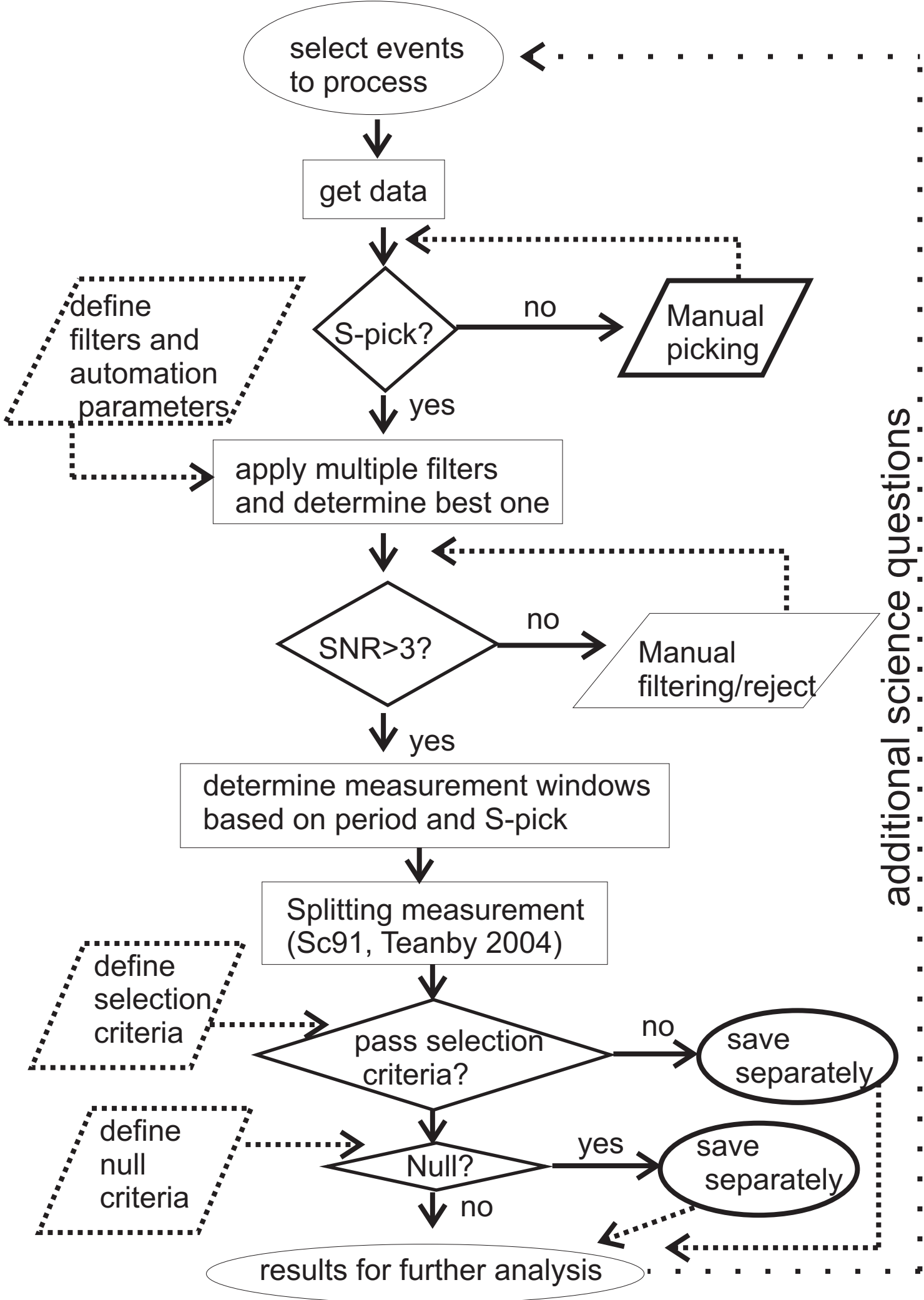


Fig. 1

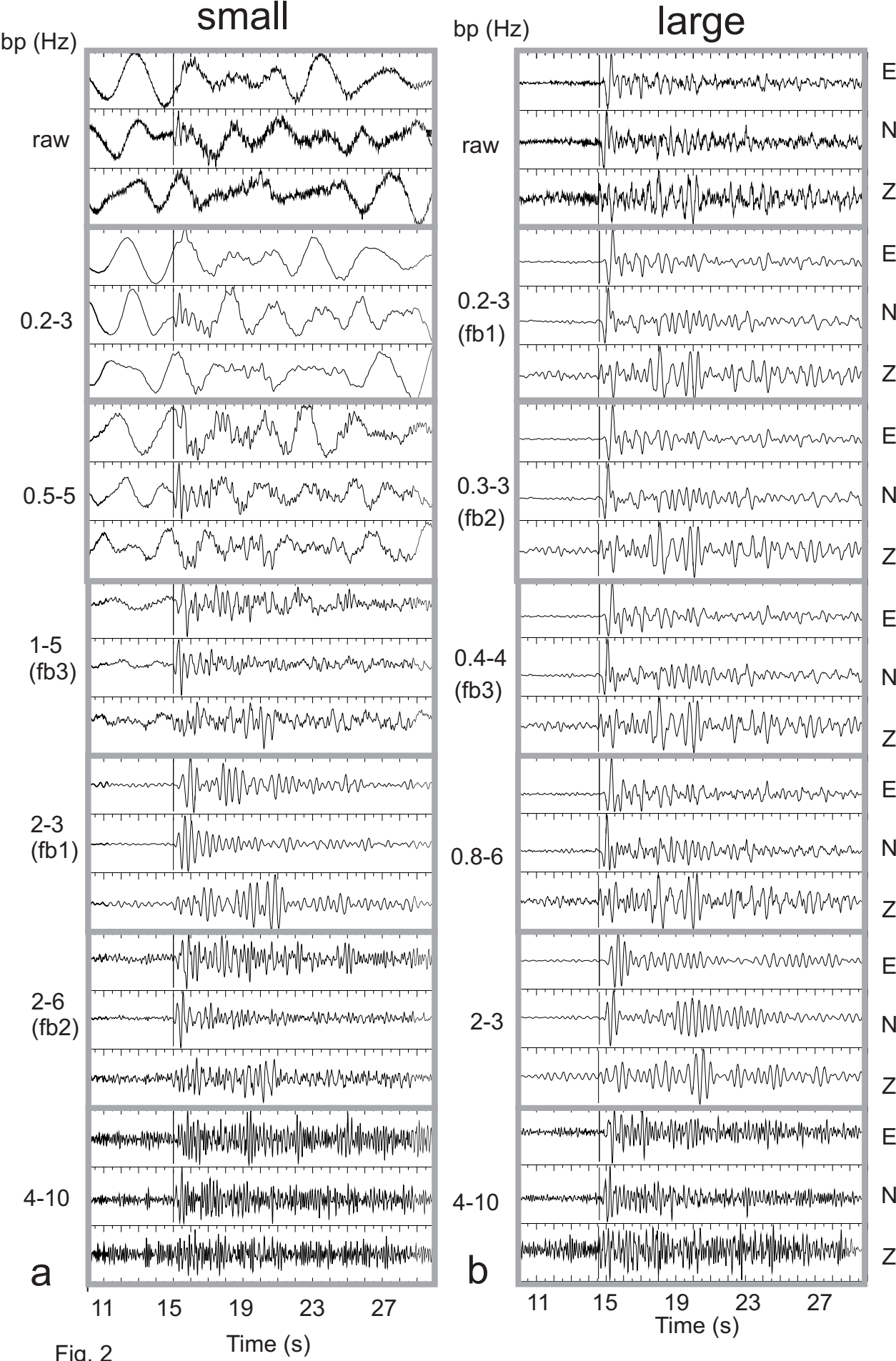


Fig. 2

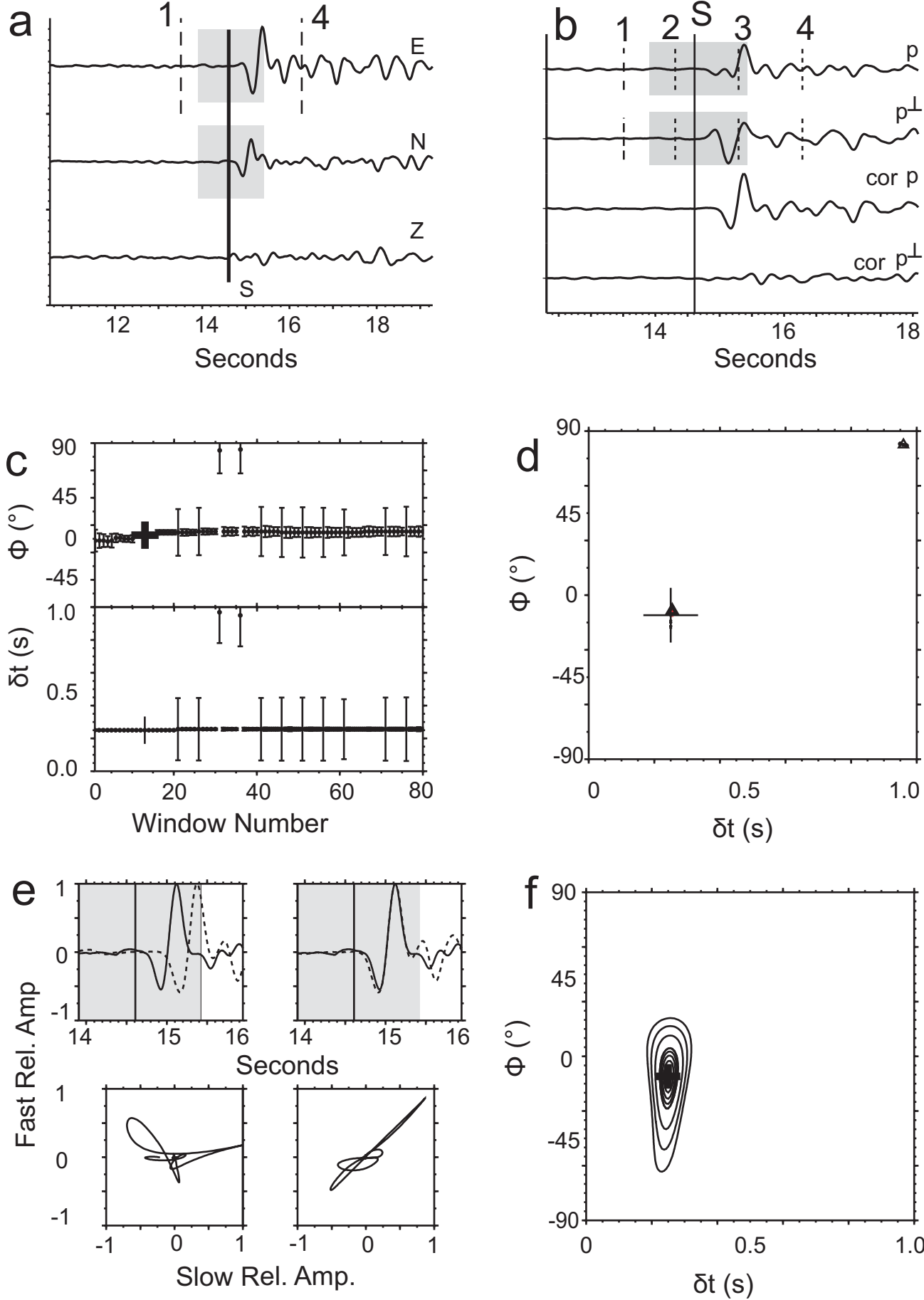


Fig. 3

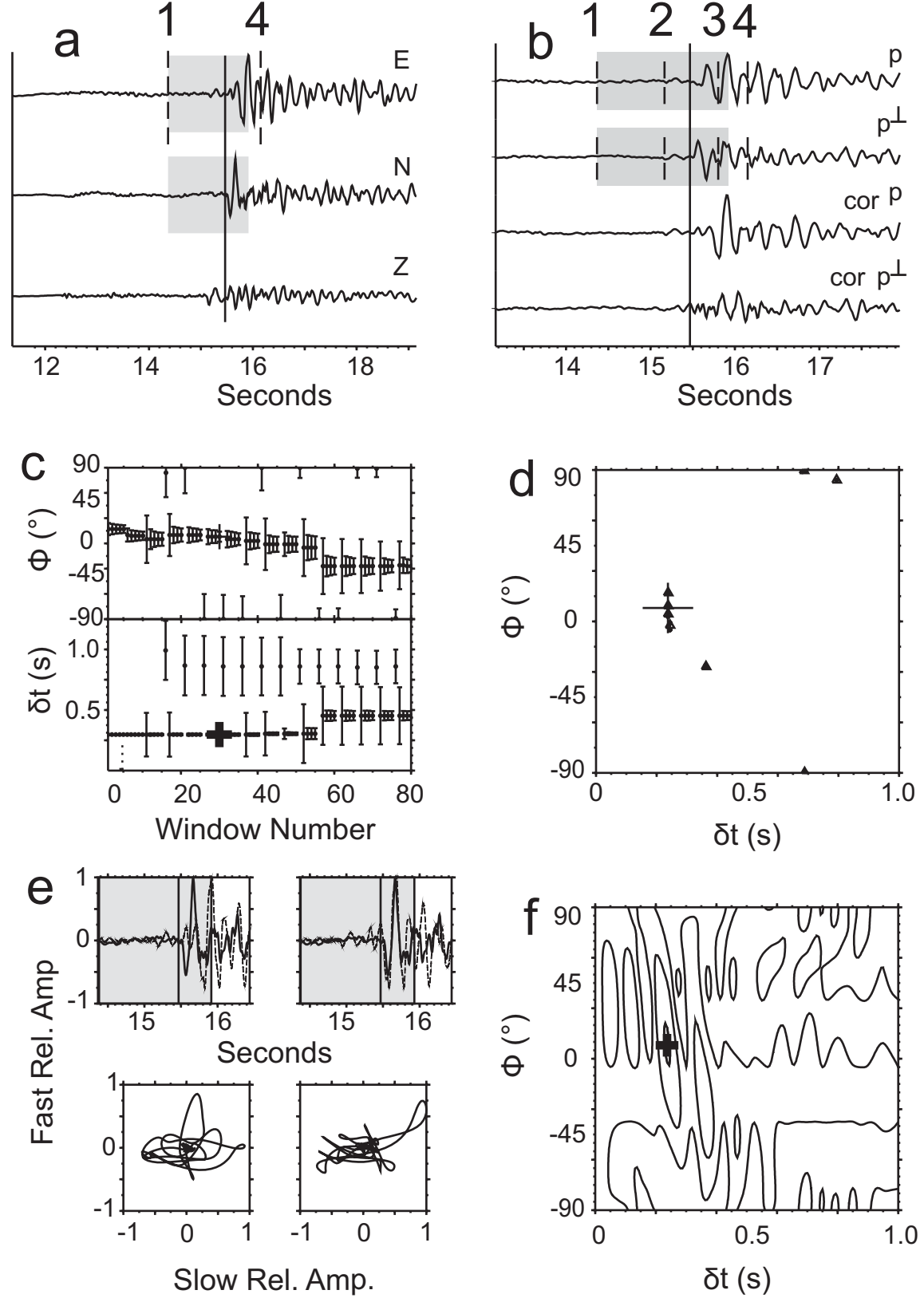


Fig. 4

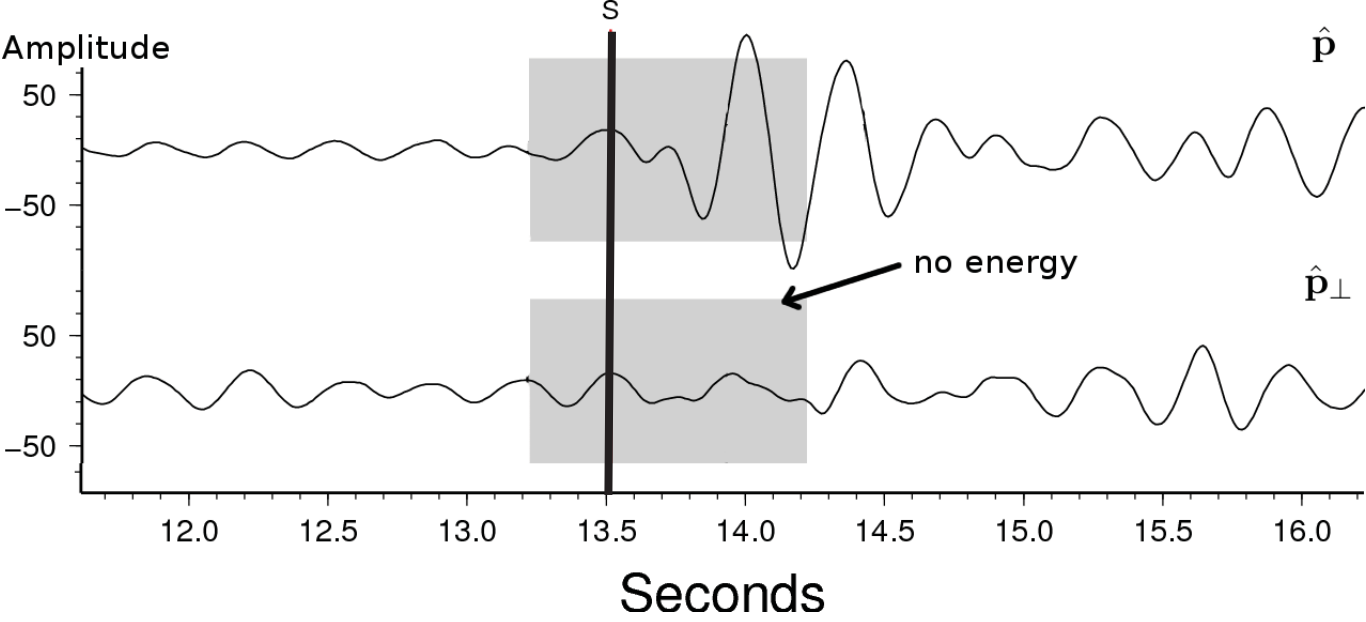


Fig. 5

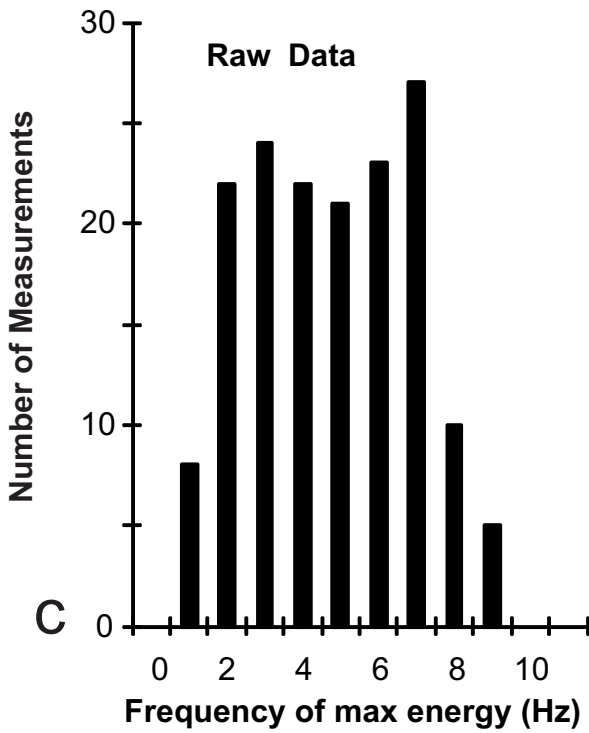
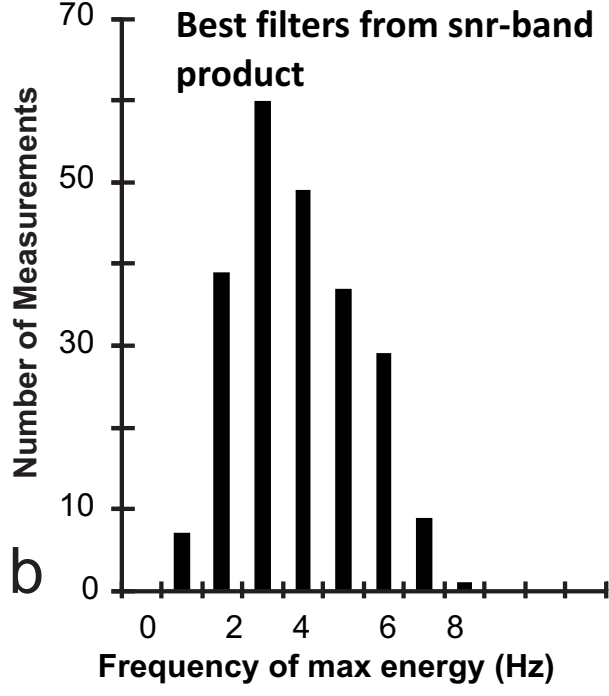
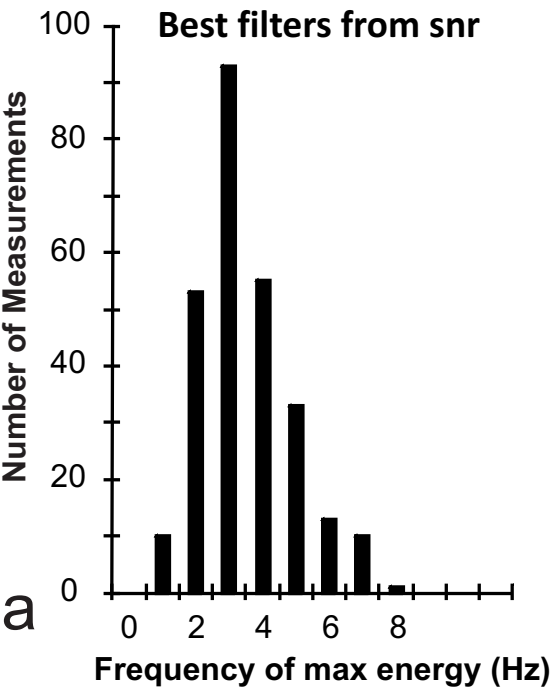


Fig. 6

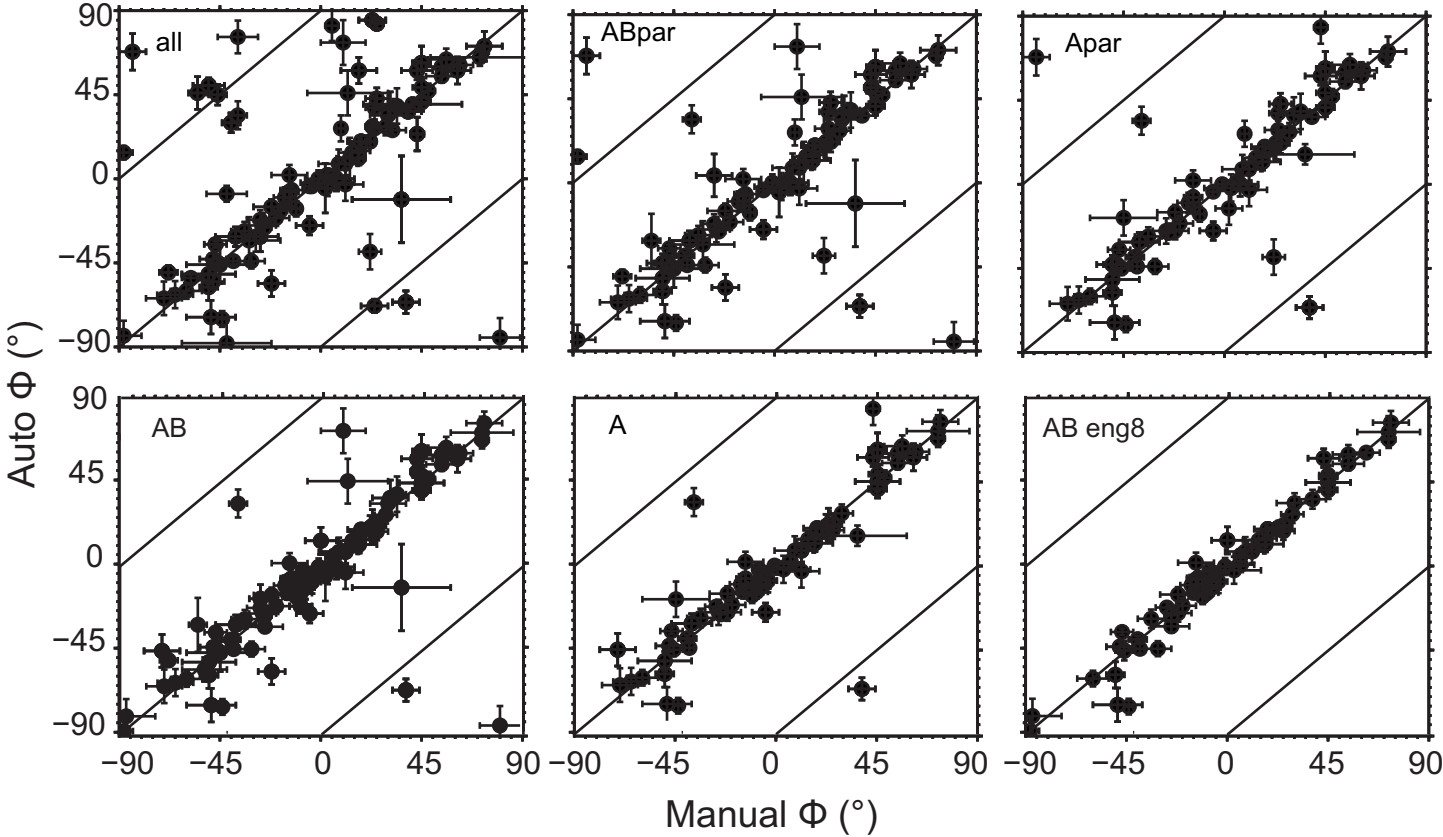


Fig. 7a

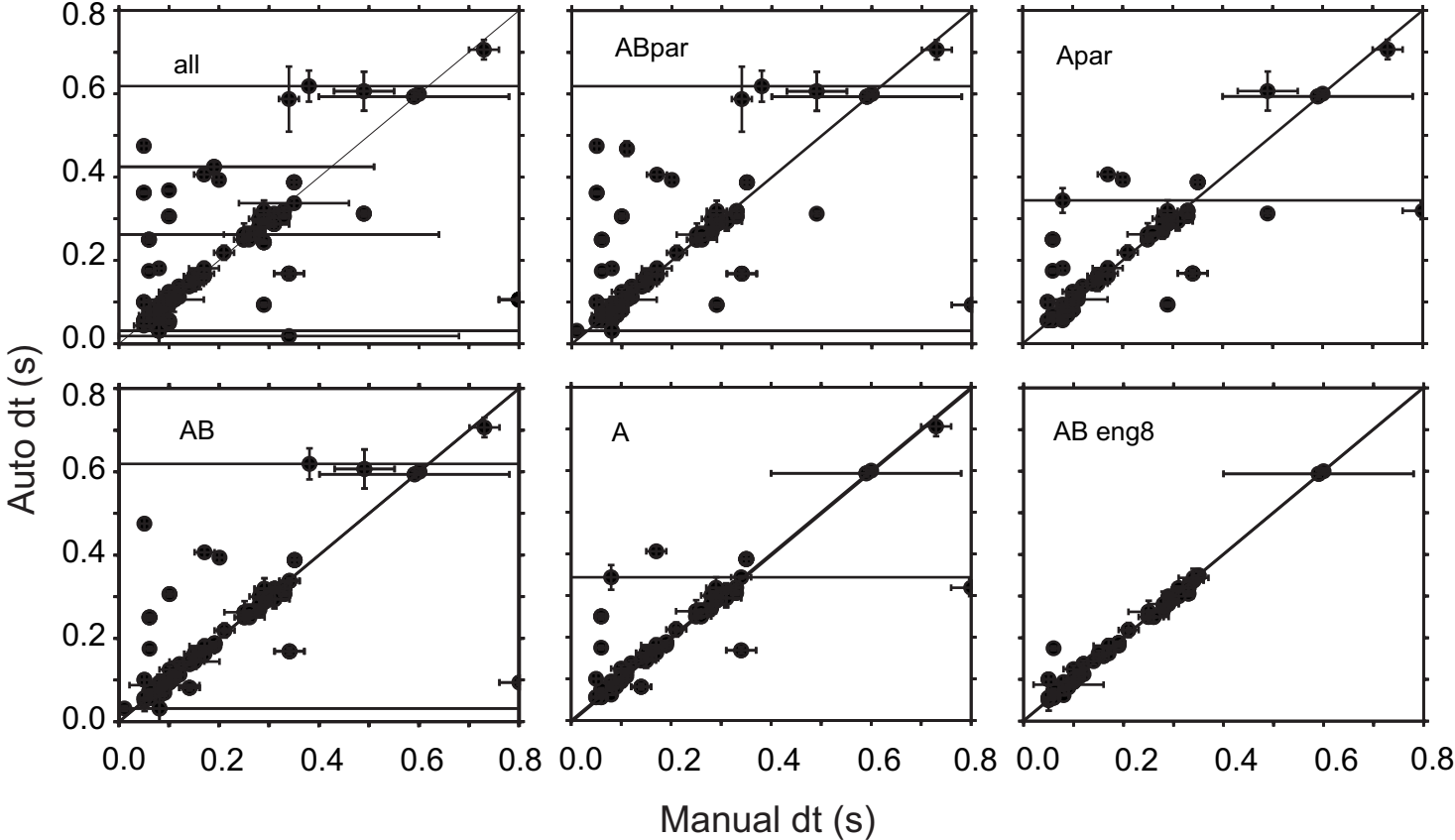


Fig. 7b

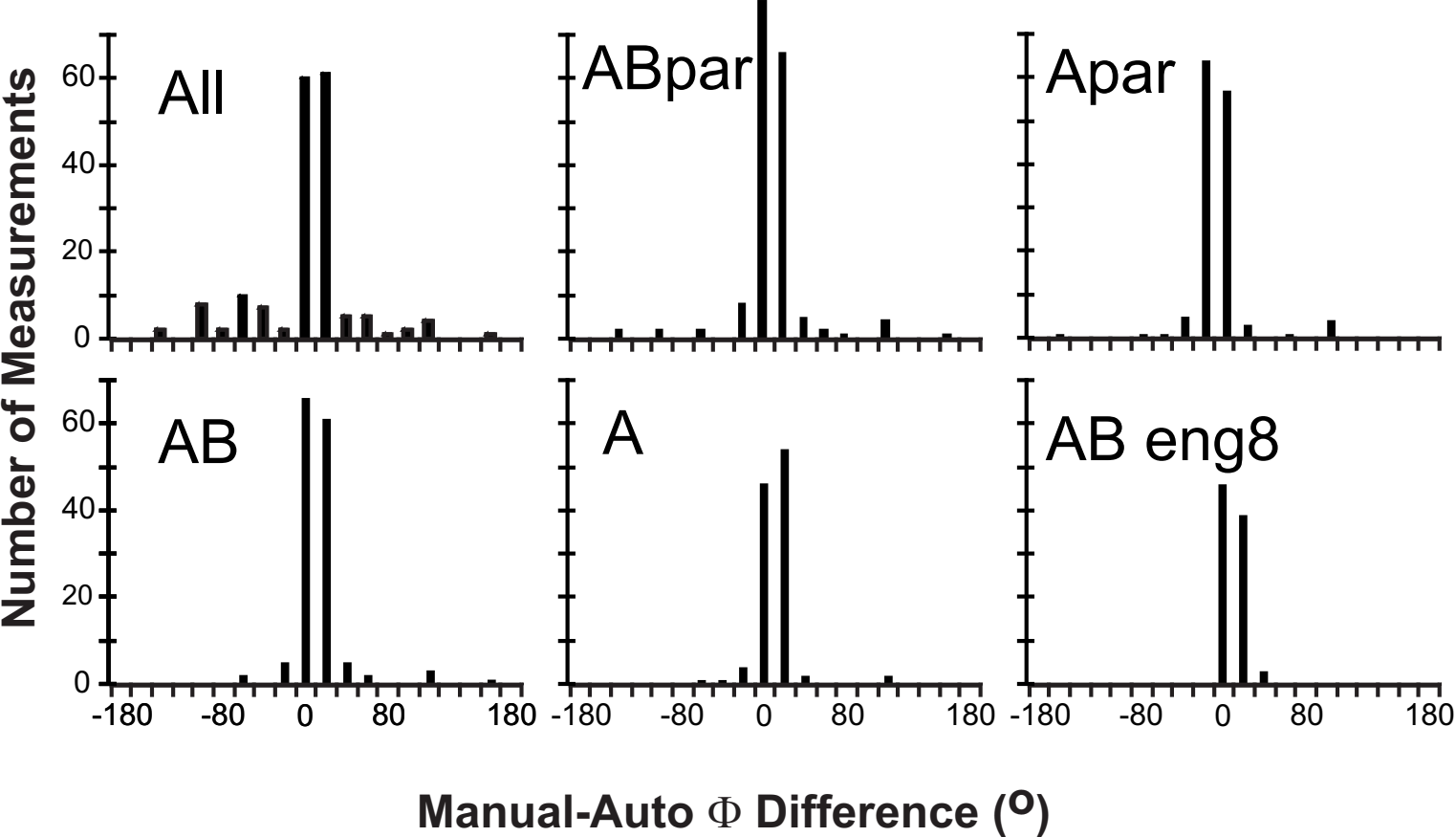


Fig. 8

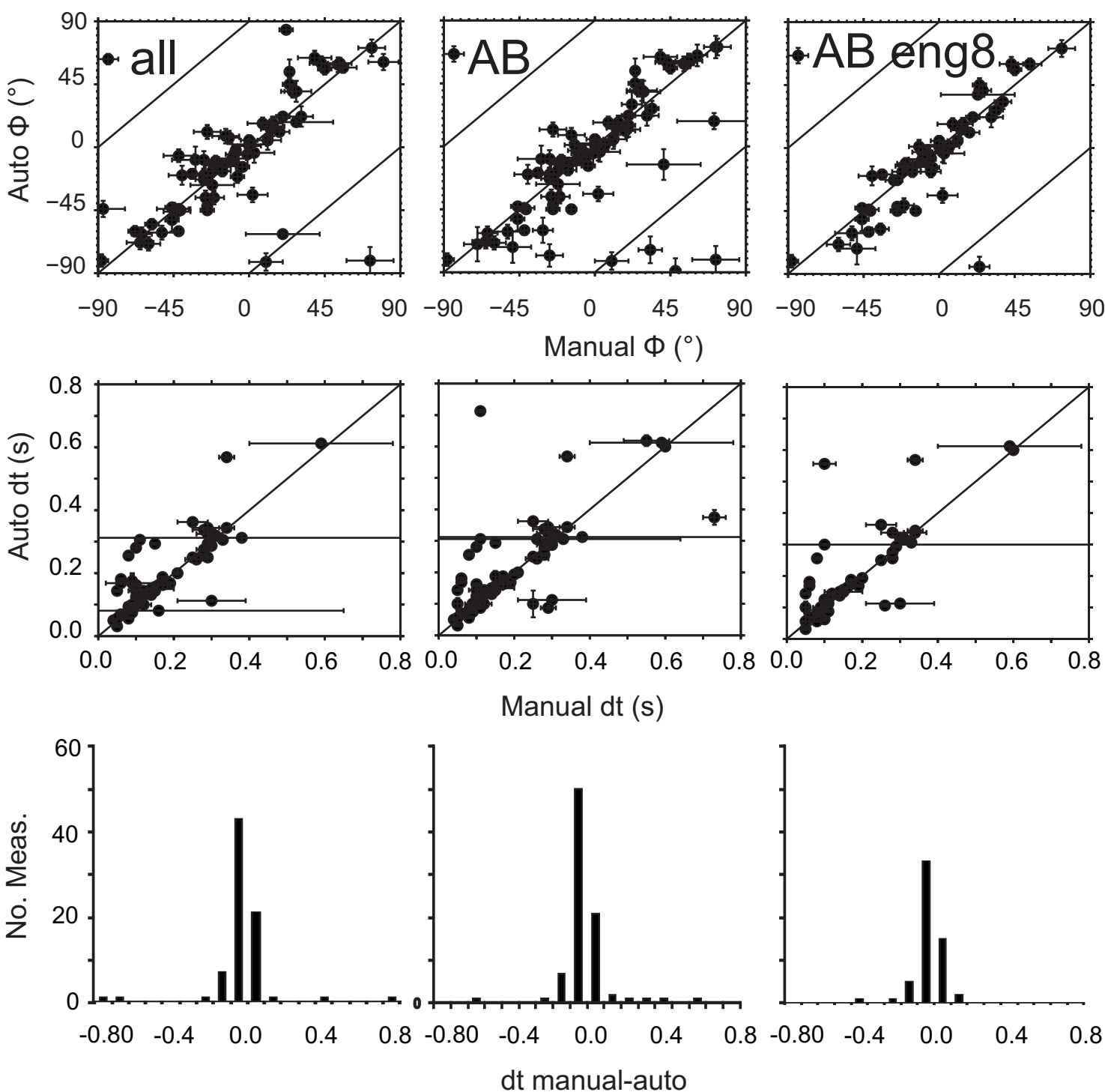


Figure 9.

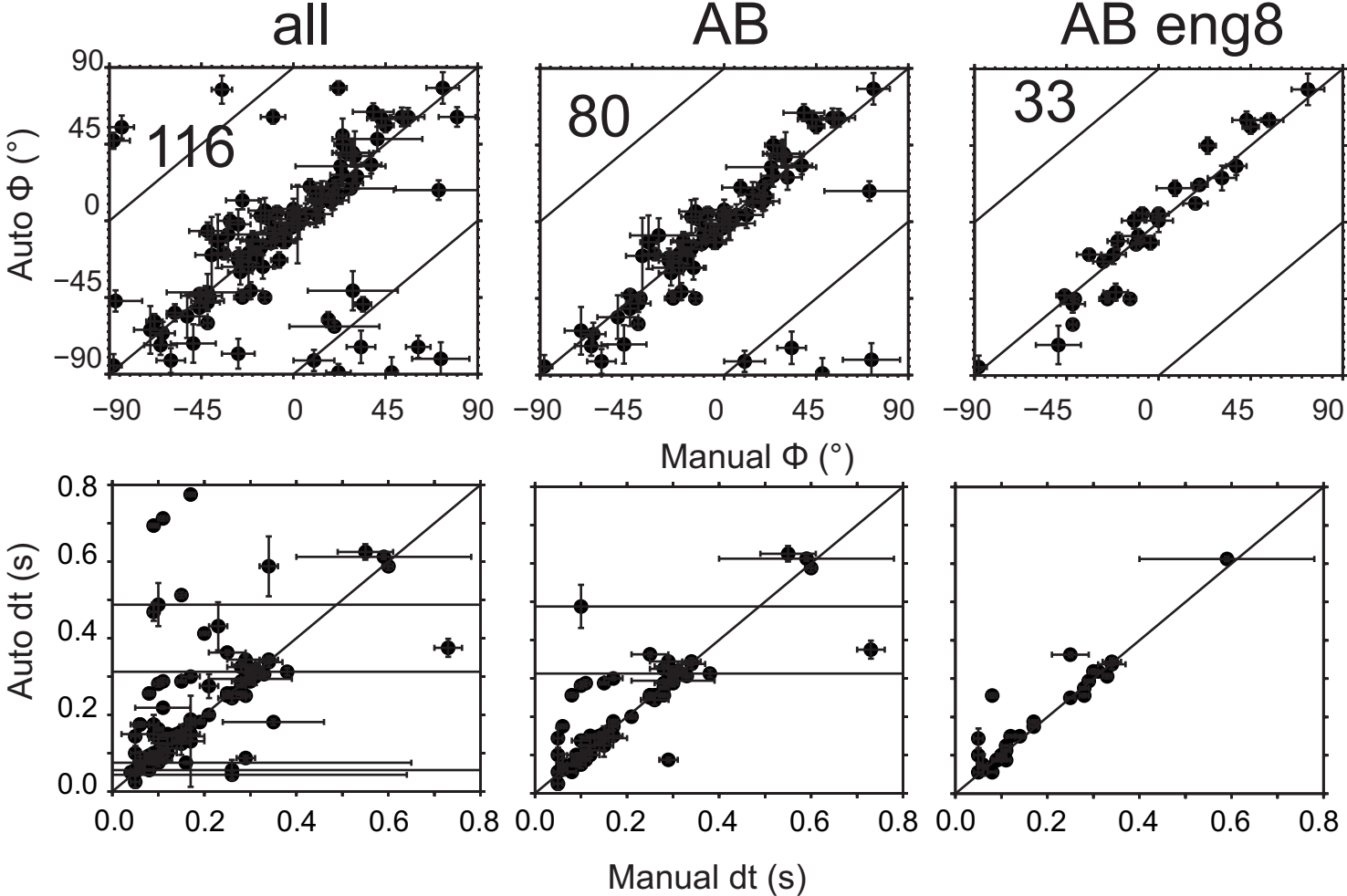


Fig. 10

manual

auto snr

auto snr-band prod

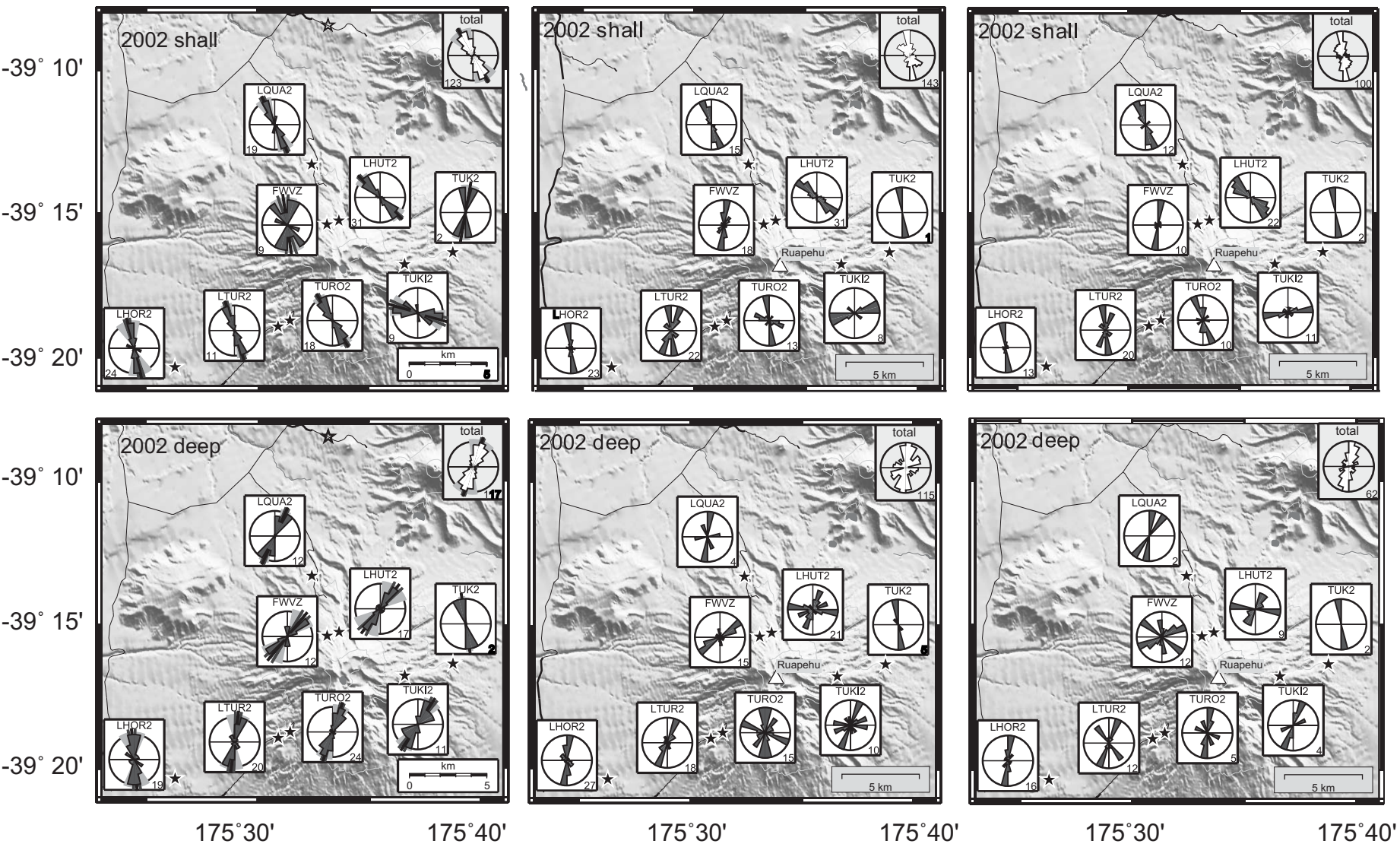


Fig. 11

manual

auto snr

auto snr-band prod

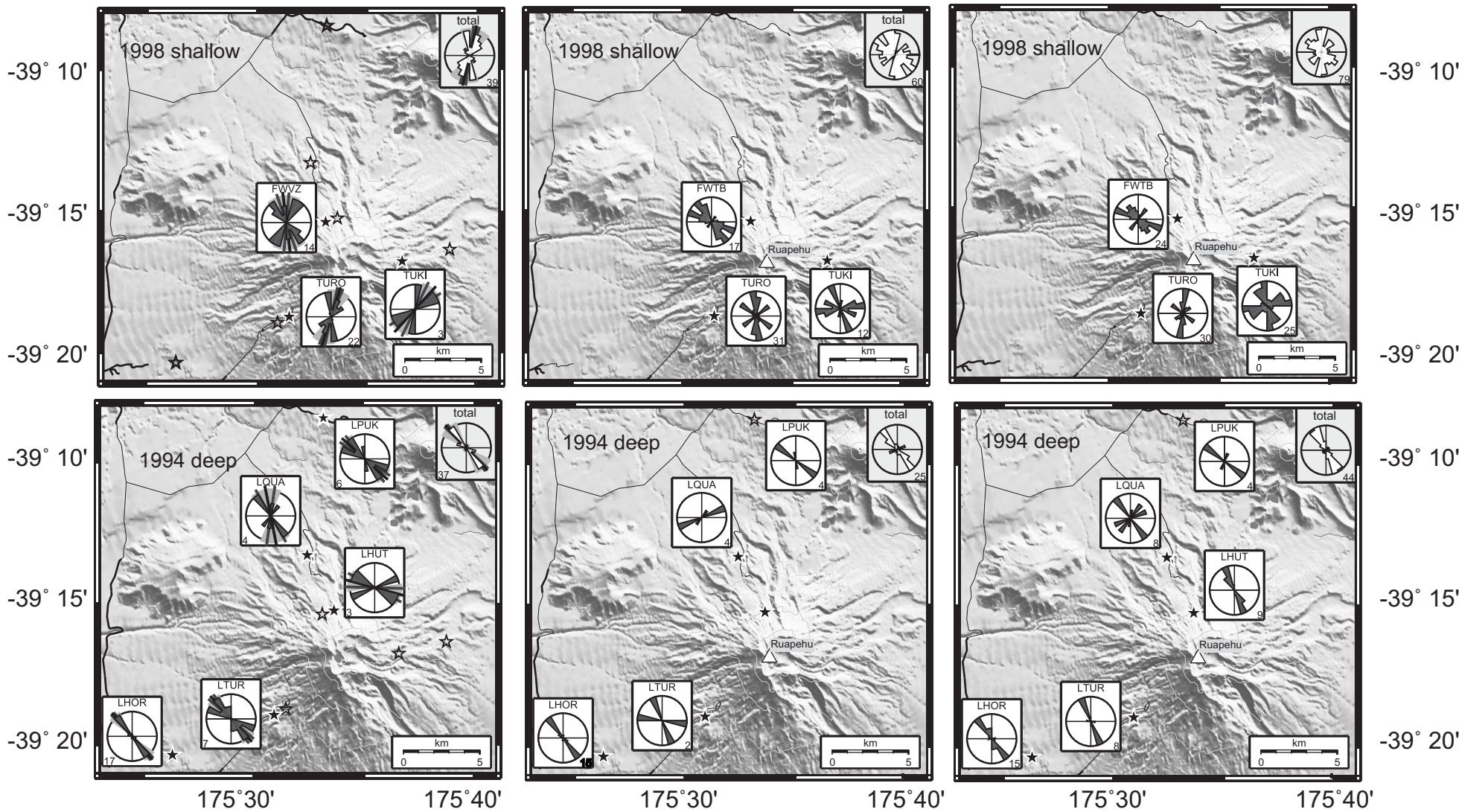


Fig 12.